ISFET pH-Sensor Sensitivity Extraction Using Conventional MOSFET Simulation Tools

Tarek M. Abdolkader, Abdurrahman G. Alahdal, Ahmed Shaker, and Wael Fikry

Abstract—The Ion-Sensitive Field-Effect Transistor (ISFET) has traditionally been used to measure hydrogen ion concentration (pH) of a solution. Its performance depends mainly on its sensitivity to pH change of the electrolyte in contact with its gate. This sensitivity is usually calculated by examining the effect of pH value on the charge and potential distributions above gate insulator, which is translated into a shift in the threshold voltage. In this work, we propose a methodology to extract the sensitivity of ISFET by linking electrolyte charge and potential equations with a device simulation tool to calculate the ISFET's drain current, thus, taking into account the underlying structure's physical properties. Using the proposed methodology, the sensitivity of ISFET is compared for various pH values and gate-insulator thicknesses searching for the optimum conditions that give the highest sensitivity.

Index Terms—ISFET, pH-sensor, biosensors, device simulation.

I. INTRODUCTION

Ion-Sensitive Field-Effect Transistor (ISFET) has been used for detection of the ionic activity in an electrolyte solution attached to the gate oxide of а Metal-Oxide-Semiconductor (MOS) structure. One of the most useful parameters to be measured in biochemistry is the hydrogen concentration, or pH. ISFET is one of the leading pH sensors using semiconductor technologies [1]. It has recently attracted more interest because of many advantages compared to other pH sensing methods such as litmus papers and glass pH electrodes [2], [3]. It has a relatively high sensitivity, smaller size, and it can be used at high temperature. Moreover, it suits continuous monitoring, has potential for large-scale integration, and may be fabricated using conventional CMOS process. ISFETs have been adopted in various lab-on-chip and health-care applications [4]. It found use also in agriculture, environmental monitoring, and food industries [2].

Fig. 1 shows a schematic illustration for the ISFET structure. It resembles normal Metal-Oxide-Semiconductor Field-Effect Transistor (MOSFET) structure except that the

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A. Shaker and W. Fikry are with the Engineering Physics Department, Ain Shams University, Egypt (email: ashaker2k@yahoo.com, waelfikry@yahoo.com). metal gate of the latter is replaced by an electrolyte solution to be tested, with a reference metal electrode immersed in this electrolyte. A change in the hydrogen ion concentration of the electrolyte (pH change) induces a change in the charge distribution on the surface of the gate insulator and this will in turn change the drain current I_D in the MOSFET [5]. pH measurement may be done by relating it to the change in drain current I_D at a fixed reference electrode voltage (V_{ref}). In this case, the sensitivity is expressed as I_D change per pH unit change. Alternatively, pH may be measured by finding the required V_{ref} shift to maintain fixed I_D value. [2]. Here, it becomes the change in V_{ref} per pH unit change.



Fig. 1. Schematic diagram of ISFET structure.

As the sensitivity of an ISFET is an important parameter determining its performance, many attempts for modeling it were reported [3], [6]-[8]. All these attempts use an approximate analytical expression to describe the electrostatics of the underlying MOSFET.

Although ISFETs have been fabricated in CMOS for a variety of physical geometries, it has not yet been reported how design dimensions impact sensor characteristics [6]. In this work, we propose a methodology for extracting the sensitivity of the ISFET using full numerical simulation of its underlying MOSFET, and thus, include the effect of MOSFET structure parameters more accurately. The proposed methodology is used to compare the ISFET sensitivity at the whole pH range, and for various current levels and reference voltage values. In addition, the effect of the gate-insulator thickness is also examined. This helps to optimize the ISFET performance by choosing the most suitable conditions of operation.

Section II reviews ISFET theory depicting its electrostatic equations. Section III presents the new proposed

Manuscript received September 25, 2014; revised January 10, 2015. Sponsor and financial support acknowledgment: This work was supported by the Deanship of Scientific Research, Umm Al-Qura University, Makkah, Saudi Arabia under Grant 43408011".

methodology. Simulation results are given and discussed in Section IV followed by the conclusion in Section V.



Fig. 2. Binding sites and double electrical layer at electrolyte-insulator interface.

II. ISFET THEORY

ISFET operation is explained using site-binding theory [9]. The insulating surface of the ISFET's gate contains hydroxyl groups (OH) that forms binding sites. They can be positively charged (by acquiring H^+) or negatively charged (by losing H^+) depending on the concentration of the hydrogen ions in the electrolyte. Accordingly, the insulating surface is charged with surface charge density that depends on the solution's pH.

According to Gouy–Chapman–Stern theory [9], electrolyte ions (anions and cations) form three regions (Fig. 2). The first extends from the Insulator-Electrolyte interface to the Inner Helmholtz Plane (IHP), which is the plane passing through the centers of the specifically adsorbed ions. Next, the region from IHP to the Outer Helmholtz Plane (OHP) that passes through the centers of the hydrated ions at their distance of closest approach to the solid. The third region consists of a diffuse charge region extending from the OHP into the electrolyte bulk, which is referred to as the Gouy-Chapman layer [7].

As shown in Fig. 3(a), the charge distribution along the *y*-direction (the direction normal to the interface) can be divided into three parts: 1) the inversion/depletion charge in the semiconductor channel, σ_{MOS} , 2) the surface charge on the Insulator-Electrolyte interface resulting from ion adsorbing, σ_{o} , and 3) the continuous charge distribution through the diffuse layer, σ_d . The corresponding potential distribution is depicted in Fig. 3(b), in which, V_{ref} , ψ_d , ψ_o , and ψ_s are the electric potentials at the reference gate electrode, the edge of diffuse layer (OHP), the electrolyte-insulator interface, and the semiconductor-insulator interface, respectively.

Applying Gauss Law using a Gaussian surface which encompasses the whole structure, we can write [5], [8],

$$\sigma_d + \sigma_o + \sigma_{MOS} = 0 \tag{1}$$



Fig. 3. (a) Surface charge density and (b) potential distribution in an Electrolyte-Insulator-Semiconductor (EIS) system along y-direction (the direction normal to the interface).

The first term in the above equation, σ_d , can be related to ψ_d and ψ_o using a Gaussian surface that encompasses the diffuse layer charge and passing through the Helmholtz layer

$$\sigma_d = C_h (\psi_d - \psi_o) \tag{2}$$

where C_h is the capacitance of the Helmholtz layer.

In addition, solving Poisson equation in the diffuse layer results in an expression for σ_d in terms of ψ_d which is given as [8],

$$\sigma_d = \sqrt{8\varepsilon_o \varepsilon_w kT c_0} \sinh\left(\frac{q (V_{ref} - \psi_d)}{2kT}\right)$$
(3)

where ε_w is dielectric constant of water, c_0 is the solution ion concentration.

Second, the surface charge density of the binding sites on the insulator interface, σ_0 , is given by [5], [8],

$$\sigma_{o} = qN_{sil} \left(\frac{[\mathbf{H}^{+}]_{s}^{2} - K_{+}K_{-}}{[\mathbf{H}^{+}]_{s}^{2} + K_{+}[\mathbf{H}^{+}]_{s} + K_{+}K_{-}} \right) + qN_{nit} \left(\frac{[\mathbf{H}^{+}]_{s}}{[\mathbf{H}^{+}]_{s} + K_{N+}} \right)$$
(4)

where $N_{\rm sil}$ and $N_{\rm nit}$ are the number of silanol sites and primary amine sites per unit area, respectively; K_+ , K_- , and $K_{\rm N+}$ are the dissociation constants for positively charged silanol sites, negatively charged silanol sites, and positively charged amine sites, respectively; $[\rm H^+]_s$ is the concentration of protons at the insulator surface. It should be noted that $[H^+]_s$ is related to the concentration of protons inside the electrolyte bulk, $[H^+]_b$ by [8]

$$\left[\mathbf{H}^{+}\right]_{s} = \left[\mathbf{H}^{+}\right]_{b} \exp\left(\frac{q\left(V_{ref} - \psi_{o}\right)}{kT}\right)$$
(5)

where the pH of the solution is $-\log([H^+]_b)$.

The third type of charge density, σ_{MOS} , is related to ψ_o and ψ_s through Gauss law

$$\sigma_{MOS} = C_{ins} (\psi_s - \psi_o) \tag{6}$$

where C_{ins} is the capacitance of the insulator.

Another equation that is needed to solve the system is the relation representing the effect of underlying MOSFET structure on the surface potential and charge density [8]

$$\sigma_{MOS} = \pm \sqrt{2\varepsilon_o \varepsilon_{Si} kT p_0} \begin{cases} \left(\frac{q\psi_s}{kT} - 1 + \exp\left(-\frac{q\psi_s}{kT}\right)\right) \\ + \frac{n_o}{p_o} \left(-\frac{q\psi_s}{kT} - 1 + \exp\left(\frac{q\psi_s}{kT}\right)\right) \end{cases}^{1/2} \end{cases}$$
(7)

where ε_{Si} is dielectric constant of silicon; n_o and p_o are the equilibrium electron and hole concentrations within silicon.

The seven equations (1)-(7) has seven unknowns: three charge densities, three surface potentials, and $[H^+]_s$, so, they can be solved simultaneously to get all potentials. Once ψ_0 is known, the shift in the threshold voltage is determined by $(V_{\rm ref} - \psi_0)$ [9], so, the new threshold voltage will be,

$$V_{T}' = V_{T} - (V_{ref} - \psi_{o})$$
 (8)

where $V_{\rm T}$ is the threshold voltage of the basic MOSFET structure. Once V_T is known, the drain to source current can be found analytically using any of the standard MOSFET models [10]. For example, simple charge control model can be used to get the drain current [3],

$$I_{D} = \frac{W \ \mu_{n} C_{ins}}{L} \times \begin{cases} (V_{G} - V_{T} - V_{D} / 2) V_{D} & V_{D} \leq (V_{G} - V_{T}) \\ (V_{G} - V_{T})^{2} / 2 & V_{D} > (V_{G} - V_{T}) \end{cases}$$
(9)

Two ways can be used to express ISFET sensitivity: the first is using S_1 defined as the absolute value of change in I_D per unit change in pH with V_{ref} fixed, so

$$S_{1} = \left| \frac{\delta I_{D}}{\delta p H} \right|_{V_{ref} \text{ (constant)}}$$
(10)

The second is using S_2 defined as the absolute value of

change in $V_{\rm ref}$ per unit change in pH that is required to maintain $I_{\rm D}$ fixed

$$S_{2} = \left| \frac{\partial V_{ref}}{\delta p H} \right|_{I_{D} \text{ (constant)}}$$
(11)

Once the drain current I_D is calculated for a certain reference voltage V_{ref} at a certain pH, I_D is found again for a neighboring pH value, and S_1 is found from (10). Similar procedure can be used for S_2 .

III. PROPOSED SIMULATION METHOD

Calculation of ISFET sensitivity presented in the last section uses approximate modeling equations to describe MOSFET electrical properties. This is represented by equations (6)-(9) which are based on simplifying assumptions to reach closed-form analytical formulae. On the other hand, numerical device simulation of MOSFET represents device physics more accurately and takes into account process effects more deeply. So, in this work, we replace these modeling equations by linking ISFET charge and potential equations (1)-(5) to the numerical device simulation tool, Silvaco [11] in order to find a complete solution of the system. The methodology is shown in the flow chart in Fig. 4 and explained hereinafter.



Fig. 4. Flow chart for the methodology proposed for the extraction of ISFET sensitivity.

At the beginning, for a certain pH of the solution, and for a

certain reference electrode voltage $V_{\rm ref}$, a value of $\psi_{\rm o}$ is assumed (roughly half of the reference electrode voltage, $V_{\rm ref}$). Then, a device simulation using Silvaco tools is performed for a conventional metal-gated MOSFET with its gate bias equals ψ_0 . From the simulation results we can calculate ψ_s , σ_{MOS} , and I_D . Now, equations (1)-(5) can be solved for the unknowns: $\sigma_{\rm o}$, $\sigma_{\rm d}$, $\psi_{\rm d}$, $V_{\rm ref}$, and $[{\rm H}^+]_{\rm s}$ and, consequently, a new value of V_{ref} is found which we call it $V_{\text{ref(cal)}}$. The calculated $V_{\text{ref(cal)}}$ is compared to the real value of the reference electrode voltage, $V_{\rm ref}$, and the difference is subtracted from the firstly assumed ψ_0 . Now, the new updated value of ψ_0 is used to perform a new simulation run. The whole process is repeated until the difference between the calculated and real values of $V_{\rm ref}$ is within a certain tolerance. After reaching a consistent solution for both ψ_0 and $V_{\rm ref}$, the drain current output from simulation is stored for the corresponding value of pH and V_{ref} .

If, conversely, the drain current $I_{\rm D}$ is predetermined and it is required to find the corresponding reference voltage $V_{\rm ref}$ that produces this current at certain pH, simulation runs are repeated with ψ_0 incremented until it produces the predetermined current, then, equations (1)-(5) are solved only once to get $V_{\rm ref}$.

All calculations are repeated for different pH values. Once $I_{\rm D}$ and $V_{\rm ref}$ are known for each value of pH, (10) and (11) can be used to calculate ISFET sensitivities S_1 and S_2 .

IV. RESULTS AND DISCUSSION

The method described in the last section was used to study the effect of various properties of ISFET pH sensor on the output current and on the two types of sensitivity defined in (10) and (11). The drain to source voltage is set to 0.2V. The other parameter values used for simulation are shown in Table I, in which, N_A is the substrate doping, L is the gate length, and W is the device width.

TABLE I: THE PARAMETER VALUES USED FOR SIMULATION

\mathcal{E}_{w}	78.3	c_0	$2 \times 10^{15} \text{ cm}^{-3}$
K_+	15.8 Mol/L	Т	300 K
K_{-}	63.1×10 ⁻⁹ Mol/L	$N_{\rm A}$	$1 \times 10^{15} \text{ cm}^{-3}$
$N_{\rm sil}$	$5.0 \times 10^{14} \text{ cm}^{-2}$	L	1.3 μm
C_h	$20 \times 10^{-6} \text{ F/cm}^2$	W	1.0 µm



Fig. 5. Drain current variation with pH value for an ISFET with gate insulator thickness $t_{\rm ins} = 40$ nm at three different values of reference electrode voltage, $V_{\rm ref} = 0.5, 1,$ and 1.5 V.

Fig. 5 shows the variation of the drain current versus pH value for SiO₂ gate-insulator of thickness $t_{ins} = 40$ nm at three

values of reference electrode voltage V_{ref} , 0.5, 1, and 1.5 V. The change in the drain current is seen to be relatively larger for small pH compared to high pH range. On the other hand, in Fig. 6, V_{ref} is plotted against pH at three current levels of 10, 13, and 15 μ A. The change in V_{ref} is also larger at low pH values. More quantitatively, in Fig. 7, the sensitivity S_1 is plotted versus pH for the same device at V_{ref} , = 0.5, 1, and 1.5 V. Although the sensitivity generally decreases with increasing pH, however, it increases again for large pH, especially for small V_{ref} . The use of large V_{ref} satisfies higher maximum sensitivity (attained at very low pH), but on the other hand, the use of small V_{ref} gives better sensitivity at very high pH. The same conclusion can be extracted from Fig. 8, in which, the other type of sensitivity S_2 is plotted versus pH for three level of drain currents, $I_D = 3$, 10, and 17 μ A. Another design factor, which is the level of output drain current, can be viewed from Fig. 8. Small current levels are suitable for large pH solutions while large current levels are better for small pH solutions.



Fig. 6. Reference electrode voltage versus pH for an ISFET with gate insulator thickness $t_{ins} = 40$ nm at three fixed current levels, $I_D = 10$, 13, and 15 µA.



Fig. 7. ISFET sensitivity, S1 versus pH value at three values of Vref, 0.5, 1 and 1.5 V for a device of gate-insulator thickness *t*ins = 40 nm. Sensitivity deteriorates for large values of pH.



Fig. 8. ISFET sensitivity, S2 versus pH value at three values of ID, 3, 10 and 17 μ A for a device of gate-insulator thickness *t* ins =40 nm.



Fig. 9. ISFET sensitivity, S_1 versus pH value at $V_{ref} = 0.7$ V and for four gate-insulator thicknesses $t_{ins} = 20, 40, 60, \text{ and } 80$ nm.



Fig. 10. ISFET sensitivity, S_2 versus pH value at $I_D = 3$ A and for four gate-insulator thicknesses $t_{ins} = 20, 40, 60, and 80$ nm.

Regarding the effect of gate-insulator thickness, Fig. 9 and 10 shows S_1 at $V_{ref} = 0.7$ V, and S_2 at $I_D = 3 \mu A$, versus pH for four values of gate-insulator, $t_{ins} = 20$, 40, 60, 80 nm. It should be noted that increasing t_{ins} has two conflicting effects, the first is to lower the sensitivity at low pH (< 10), and the other is to increase the sensitivity at high pH (> 10). On the average, increasing t_{ins} will improve the sensitivity of the device as a whole and guarantees a higher lower limit on the whole pH range. This will be on the expense of the decrease of output drain current.

V. CONCLUSION

A new methodology was proposed to extract the sensitivity of ISFET pH sensor. The methodology links charge and potential equations in the tested solution with a device simulation tool to account for MOSFET electrical properties. An initial guess for the potential at the insulator surface is assumed, then, simulation is performed to find the corresponding value of the external reference electrode voltage. The process is repeated until the calculated value is consistent with the real applied reference voltage. Various effects on ISFET sensitivity were investigated such as drain current level, reference voltage, pH range, and gate insulator thickness. It is found that the sensitivity is generally higher for low pH values. It is also found that working at low current levels and larger gate insulator thicknesses decreases the maximum sensitivity (at low pH), but on the other hand it gives the advantage of increasing the minimum sensitivity (at high pH).

ACKNOWLEDGMENT

The authors would like to thank Deanship of Scientific Research at Umm Al-Qura University for the financial support of this project under the grant number 43408011.

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International Journal of Chemical Engineering and Applications, Vol. 6, No. 5, October 2015



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